#### **Supplemental Slides for:**

Using STELLOPT/REGCOIL and to find a better winding surface for QHS46 and

Part 2: Discrete coils, free-boundary VMEC MHD solutions and Poincaré plots

With some bug fixes to plots and other typos

John C. Schmitt

A. Bader, H. Frerichs, M. Landreman, S. Lazerson, E. Paul







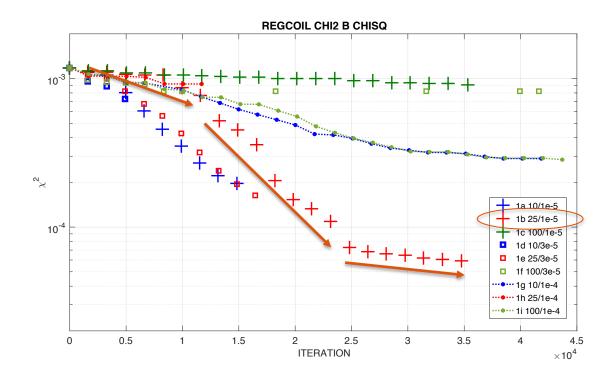


### Backup Slides



# The next 21 slides show the evolution of the new 'optimal' solution during case 1b with FACTOR/EPSFCN = 25 / 1e-5

- This is the case shown in red '+' symbols, see arrows
- The first slide will explain what is being shown in each subplot
- There are 21 set of plots, one for each new solution

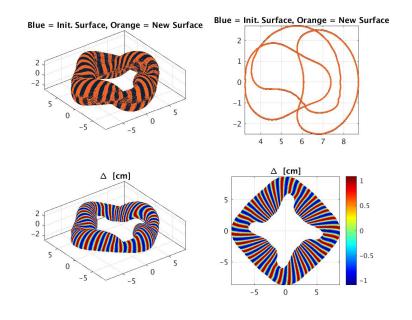


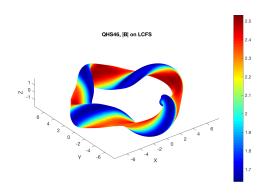


#### As an example, the first step (but don't dwell on it)

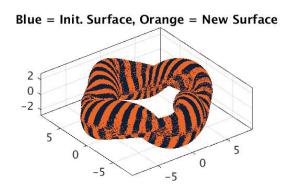
- X, Y, Z axis units are meters
- Upper Left: The original winding surface (in black) and the new winding surface (orange) are superimposed on the same axes. This allows a simple 'binary' eye inspection to see the gross features of the surfaces
- Upper Right: Planar slices of the winding surface at  $\zeta = (0^{\circ}, 45^{\circ}, 90^{\circ}) * \frac{360^{\circ}}{NFP}$
- Lower left and right: The distance (in cm) from the new surface to the original surface, multiplied by the sign of the change in the vertical (Z) –direction
- Original target |B| on target LCFS also shown for reference
  - This is not a 'self-consistent' |B|

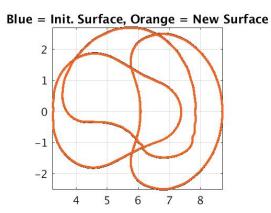
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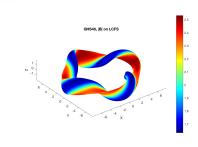


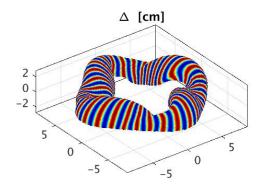


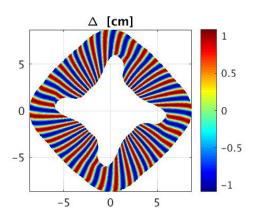
#### Iterative solution #2, The first step







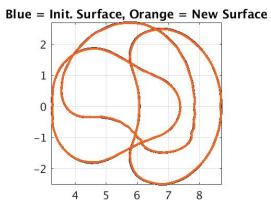


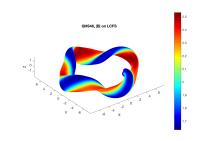


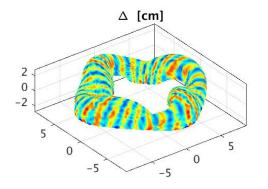


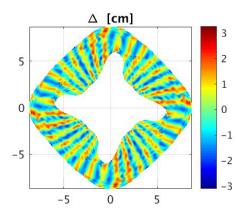
Blue = Init. Surface, Orange = New Surface

-5



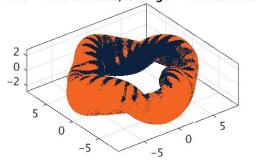




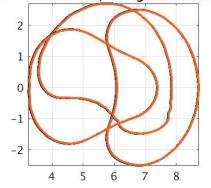


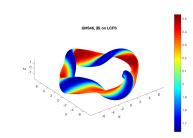


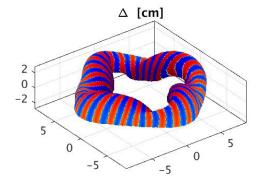
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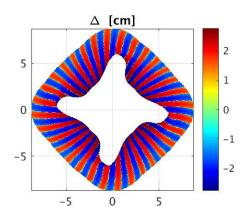


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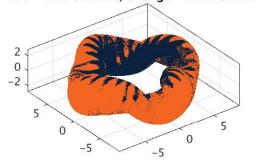




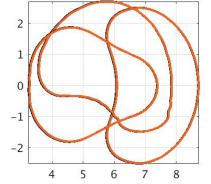


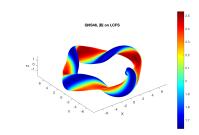


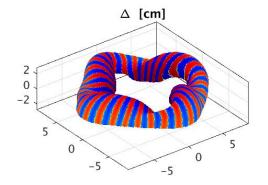
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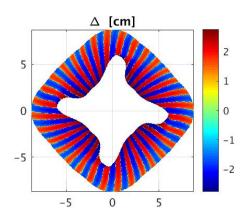


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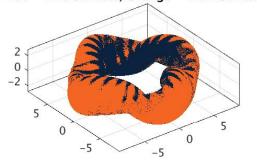




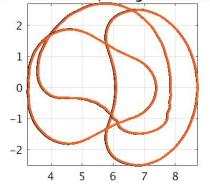


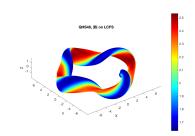


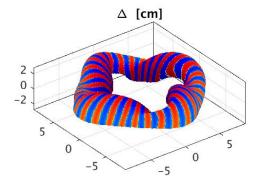
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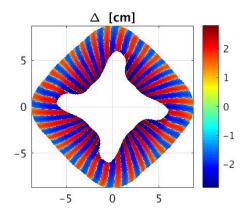


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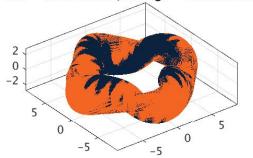




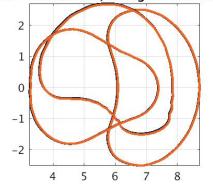


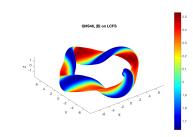


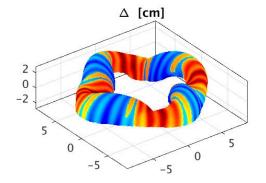
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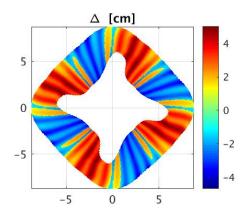


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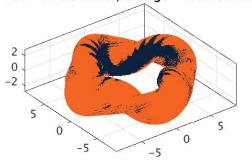




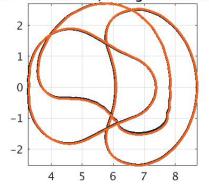


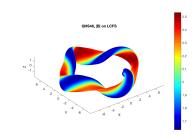


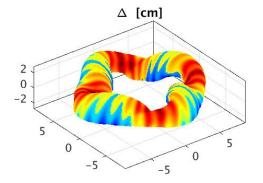
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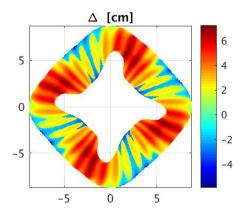


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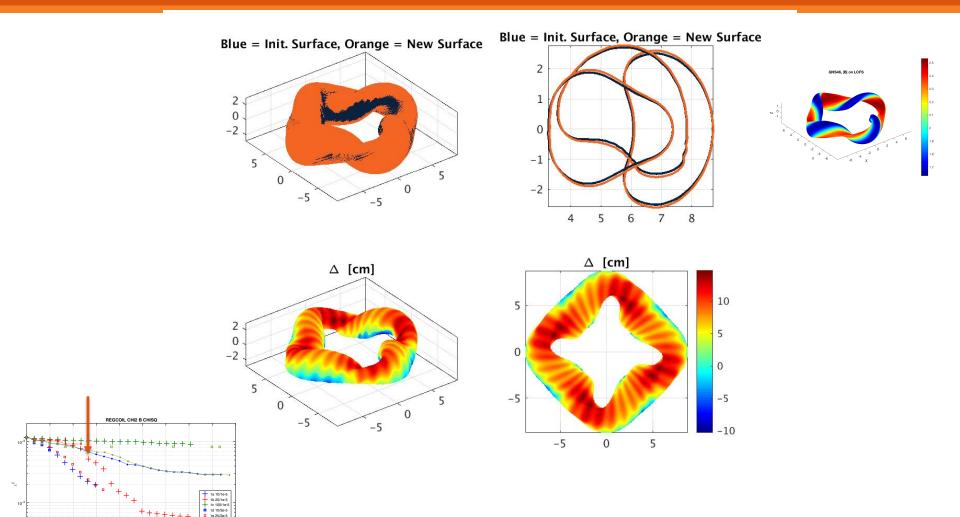




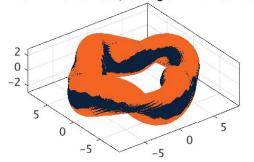




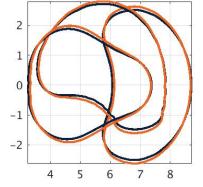
# Iterative solution #9: A new rate of descent begins now; Surface will become narrower and taller.

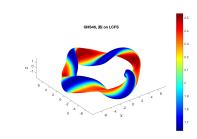


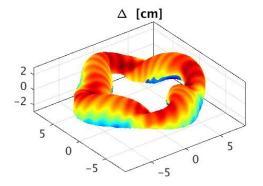
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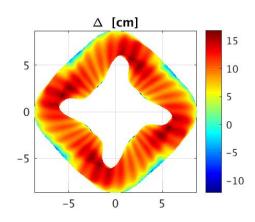


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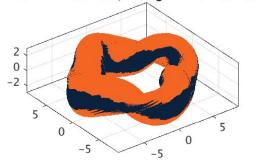




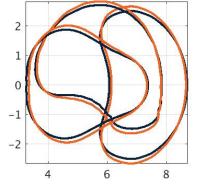


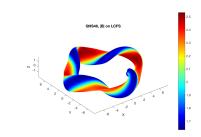


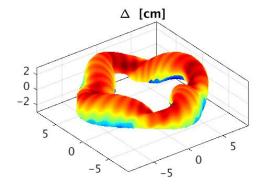
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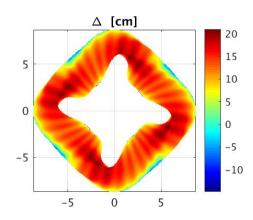


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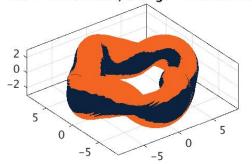




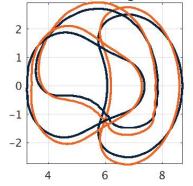


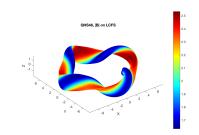


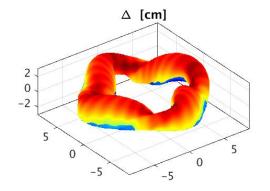
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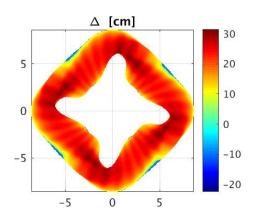


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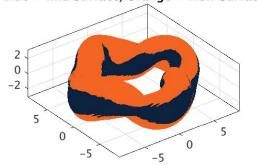




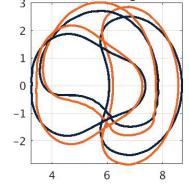


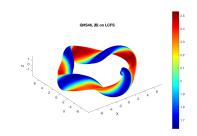


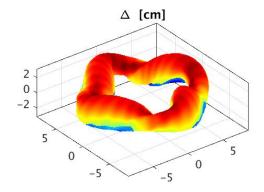


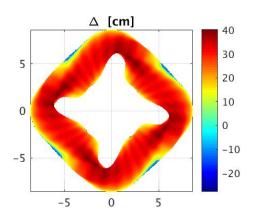


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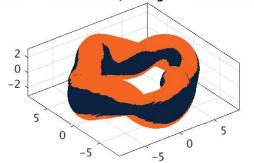




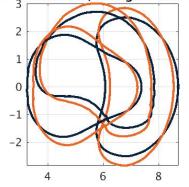


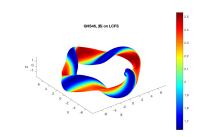


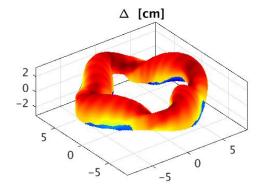


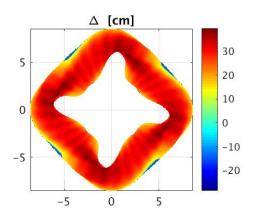


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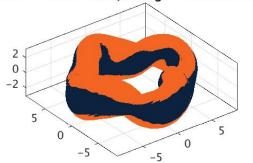




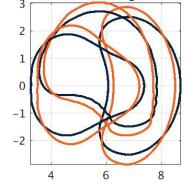


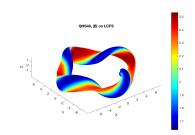


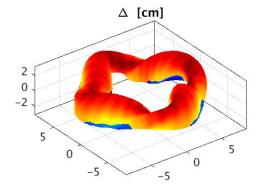
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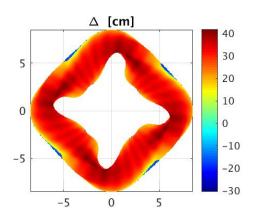


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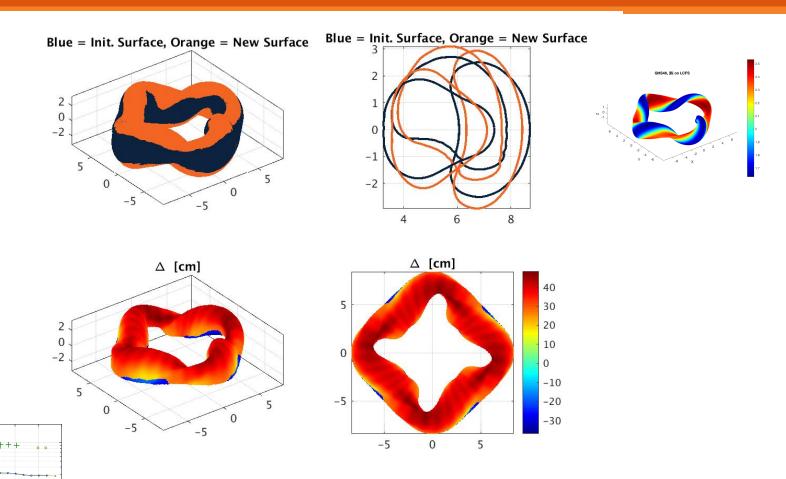


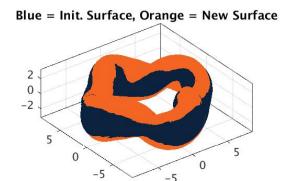


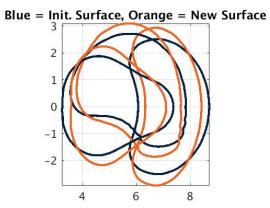


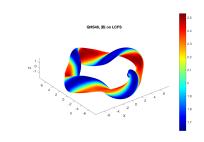


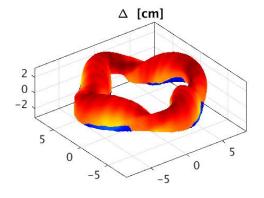
# Iterative solution # 16: Descent slows down from here on to the end

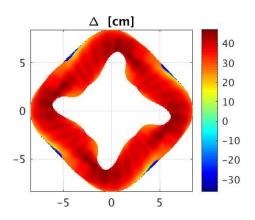




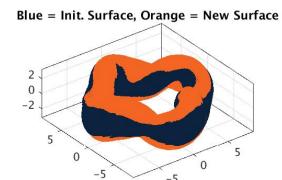


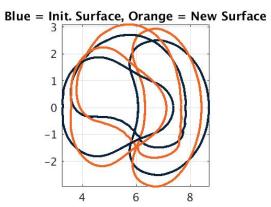


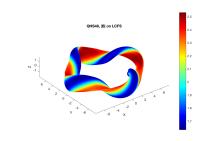


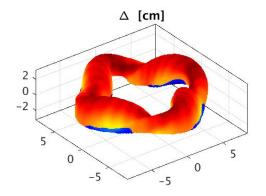


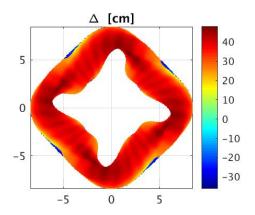




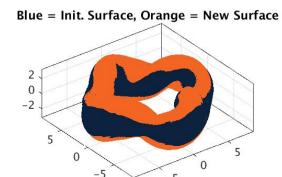


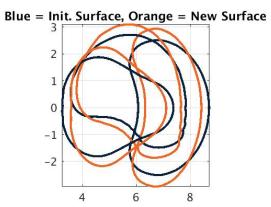


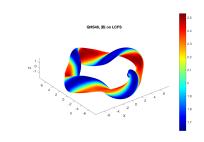


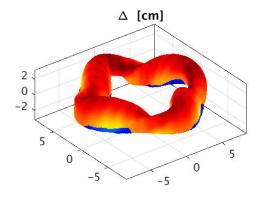


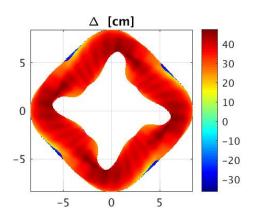




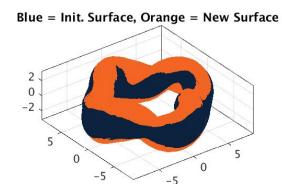


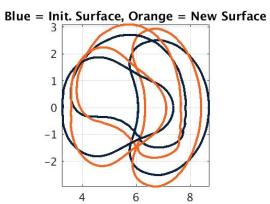


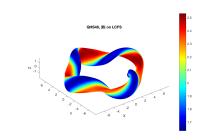


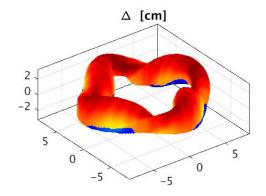


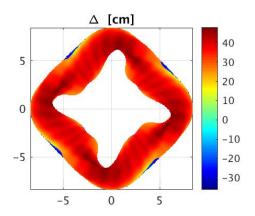




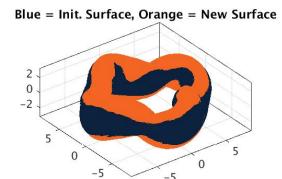


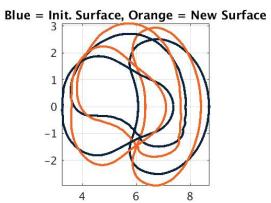


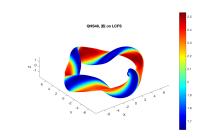


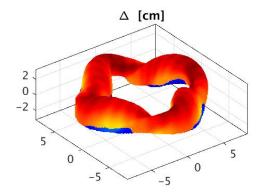


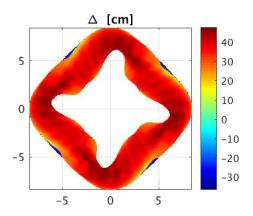








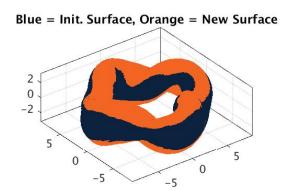


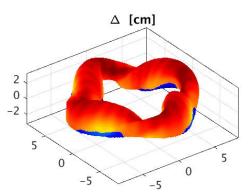


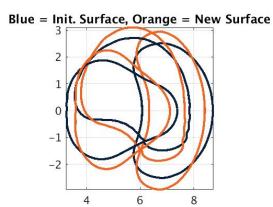


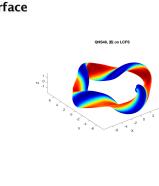
#### Iterative solution #22: (24x32 cpu-hour time limit)

- The solution after the last iteration is teller and narrower than the starting position
- Recall: The starting position was a 'uniform distance' away from the plasma boundary









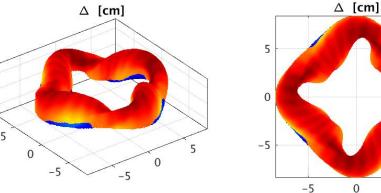
40

30 20

10

0 -10

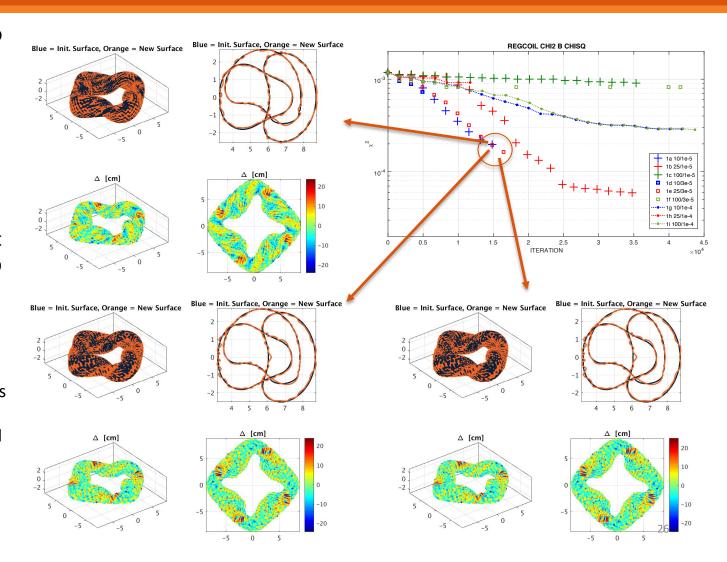
-20 -30





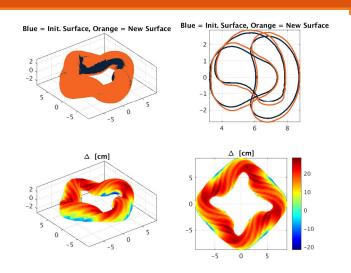
# The optimizer runs that demonstrated the most rapid descent A) look a little different, B) are still evolving, and C) terminated because the solver was in a local minimum (I think)

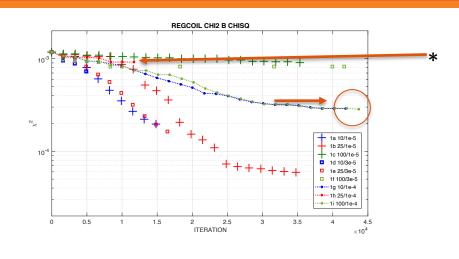
- The surfaces of the two branches that descend more rapidly, but are truncated, look a little different
- blue +'s (upper left)
- red squares (lower left)
- The red square descent path has one extra step
  see lower right plots
- ➤ The solver got stuck in a local minimum?
  - "algorithm estimates that the relative error between x and the solution is at most xtol"

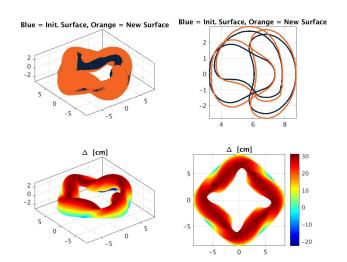


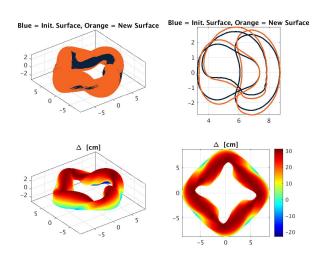


# The optimizer branch that descends more slowly looks vaguely like the 'best' case: Taller, **but less narrow**!











# Helical Stripes: The runs that descend very slowly has very corrugated surfaces.

